

is not the issue, the complexity is the issue. • DFT has complex calculations. DCT do not have • DFT has poor energy compaction, etc. · DCT has been developed by Ahmed Nootarajan & Rao 1974. • The DCT is the member of the fumily of real Valued discrete sinnsofdert unitary Tourstons. unitary >> A A = I. The discrete cosine transform consists of a set of busis vectors that are cosine functions. · PCT is a technique for converting a signal into elementary trequency components and is widely used in image compression · DCT is used in JPEG for compossion (His very Jupt). The ability to pack energy of the spatial sequence into as few trequency coefficients as possible is called as Energy compaction. • If compaction is highgive only have to transmit a few coefficients, instead of the whole of pixels. • To perform the JPEG coding, an image (in color/gray) rig first subdivided Parto blocks of <u>8x8</u> pixels. • The discover Cosine Truni (DCT) is then performed on each block. • This generates <u>64</u>' wefficients which are the quantized to reduce their magnitude. • The coefficients are then recorded into a one dimentional array in a zigzag manner before further entropy encoding. • The compression is achieved in two stages : the first is during quantization and the second during entropy coding process. • invels • invels s



# The 22, DCT and its inverse (IDCT) of ave shown below:- $J = \frac{2}{N} C(u)C(v) \sum_{\chi=0}^{N+1} \frac{f(\chi,y)}{2N} \frac{f(\chi,y)}{2N} \frac{f(\chi,y)}{2N} \frac{f(\chi,y)}{2N} \frac{f(\chi,y)}{2N}$ Fluiv 2010 CT:-fory) =  $\frac{2}{N}C(u)C(v) \stackrel{N+}{\leq} \stackrel{N+}{\leq} F(u,v)G_{s}[\underbrace{G_{s}(+)}] \stackrel{ut}{=} G_{s}[\underbrace{C_{2}g_{H}}] \stackrel{vt}{=} \underbrace{G_{s}}[\underbrace{C_{2}g_{H}}] \stackrel{vt}{=} \underbrace{G_{s}}[\underbrace{C_{s}}] \stackrel{vt}{=} \underbrace{G_{s}}[\underbrace{G_{s}}] \stackrel{vt}{=} \underbrace{G_{s}}[$ 

. Despite excellent energy compaction capabilities, DCT offers

a few limitations which restrict its use in vory low bit rate applications. Torincation of higher spectral coefficient results in <u>bluoring</u>. If the images, especially wherever the details are high. Coarse quantization of some of the low spectral coefficients introduces graininess in the smooth portions of the images. Serious blocking artifacts are introduced at the block

boundaries, since each block is independently encoded, often with a different encoding strategy and the extent of quentization. > The NXN cosine forms form matrix  $C = \{C(u, v)\}$  also called the Discrete cosine (function) toursform-DCT is defined as- $C(u,v) = \int \frac{1}{\sqrt{N}} \quad i \quad (u=v), \quad (\leq v \leq c N+1), \quad (o \leq v \leq 3)$  $for NXN=4XY \left[ \sqrt{\frac{2}{N}} \cos\left[\frac{1}{2N+1}\right] \frac{1}{2N} \le u \le (N-1) - \frac{1}{1 \le u \le 3} \right]$ 4-050.5 0.5 0.5 0.5  $C(0,0) = \frac{1}{\sqrt{4}} = 0.5$ 10.65 0.27 -0.27-0.65  $C(0,1) = \frac{1}{\sqrt{4}} = 0.7$ 2/0.5 -0.5 -0.5 0.5 C(0,2)2 1 = 0.5 3 0-27 - 0.65 0.65 - 0.27  $CCO, 3) = \frac{1}{15} = 0.5$ N20, C(1.0) 2 C(1.1) J to be contd... C(1.1) J to be contd... on Next page (25) 2

 $C(uv) = \sqrt{2} \cos \pi (2v+1) u$ ; for  $154 \le N+1$ for all w; 15453  $C(1,0) = \sqrt{\frac{2}{4}} \cos(\frac{\pi + 1}{2x4})^{1}$  $C(110) = \sqrt{\frac{1}{2} \cdot \cos(\frac{11}{8})} = +0.6532.$  $C(11) = \sqrt{\frac{2}{4}} \cos \pi \frac{(2+1)1}{2(\sqrt{4})} = \sqrt{\frac{1}{2}} \cos \left(\frac{3\pi}{8}\right) = + \frac{1}{2(\sqrt{4})} = 0.2705$  $C(1,2) = \sqrt{\frac{2}{4}} \left( \cos \pi \left( \frac{4+1}{1} \right)^{-1} = \sqrt{\frac{2}{2}} \cdot \left( \cos \left( \frac{5\pi}{8} \right) \right) = \frac{15\pi}{15\pi} - \frac{15\pi}{15\pi$  $C(1,3) = \sqrt{\frac{2}{4}} \log \frac{T(6+1)!}{6+1!} = \sqrt{\frac{2}{2}} \log \frac{T(6+1)!}{6} = \sqrt{\frac{2}{4}} \log \frac{T(6+1)!}{6} = \sqrt{\frac{2}{4}} \log \frac{T(6+1)!}{6} = \sqrt{\frac{2}{4}} \log \frac{2}{6} \log \frac{2}{6} = -0.6532$ uuy C(3,0) = 0.2705 $UUY_{C(2,0)} = 0.5$ C(3, 1) = -0.6532C(211) = -0.5C(3, 2) = 0.6532C(2,2) = -0.5C(3, 3) = -0.2705C(2,3) = 0.5\* Propensies of DCT 1. The cosine transform is real and orthogonal, ie  $c = c^{\star} = \tilde{c} = c^{\dagger}$ 

The cosine transform is not the real part of the unitary DFT. However, disine transform of a sequence is related to the DFT of its symmetric extension.
The cosine transform is fast transform.
The cosine transform of a vector 'N'elements can be calculated. (Nlog N) operations via <u>N°Pt</u>. FTT.
The cosine transform has excellent energy compaction 2

for highly correlated data. 5. Many of Loefficients are small, ie most of the energy of duty is packed in a few transform coefficients. forman and g